



# King Fahd University of Petroleum & Minerals

College of Computer Science and Engineering

Information and Computer Science Department

First Semester 142 (2014/2015)

## ICS 202 – Data Structures

### Final Exam

Monday, May 25<sup>th</sup>, 2015

Time: 120 minutes

Name: \_\_\_\_\_

ID#

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Section 01 Dr. Sami	Question #	CLO	Max Marks	Marks Obtained
	1	3	25	
	2	4	35	
Section 02 Dr. Ramadan	3	4	20	
	4	4	20	
	Total		100	

### Instructions

1. Write your name and ID in the respective boxes above and circle your section.
2. This exam consists of 10 pages, including this page, plus one reference sheet, containing 4 questions.
3. You have to answer all 4 questions.
4. The exam is closed book and closed notes. No calculators or any helping aids are allowed.
5. Make sure you turn off your mobile phone and keep it in your pocket if you have one.
6. The questions are not equally weighed.
7. The maximum number of points for this exam is 100.
8. You have exactly 120 minutes to finish the exam.

1 **Note:** this solution has been made by a student, so it's may have some mistakes :) I hope you do well in all of your final exams

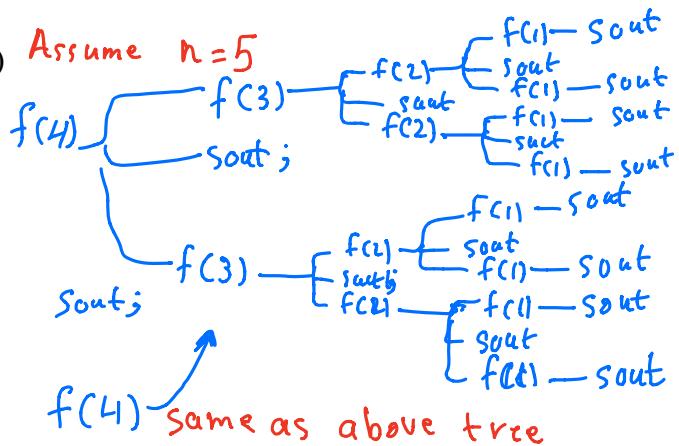
sure

**ملاحظة :** هذا الحل من عمل طالب من الممكن يكون هناك بعض الأخطاء

**Q.1 [25 points] Multiple Choice Questions:** Mark the best answer for each question below.  
**Note:** only one choice should be chosen.

1. Consider the following recursive function  $f(n)$

```
public static void f(int n)
{
    if (n == 1)
        System.out.println(n);
    else{
        f(n - 1);
        System.out.println(n);
        f(n - 1);
    }
}
```



The number of times the printing statement is executed for the method  $f(n)$  is:

- a.  $n^2$  25  
b.  $n^2 - 1$  24  
c.  $2^n$  32  
**d.  $2^n - 1$  31**  
e. none of the above.

if we see above there is 31 printing  
if we try the choices we see that d  
satisfy the number of printing statements

2. Consider the following code segment

```
for (int i=1, sum=0; i<n-1; i++)
    for (int j=i-1, sum=0; j<i+1; j++)
        sum+=4; // Statement 1
```

The complexity of the above code segment is

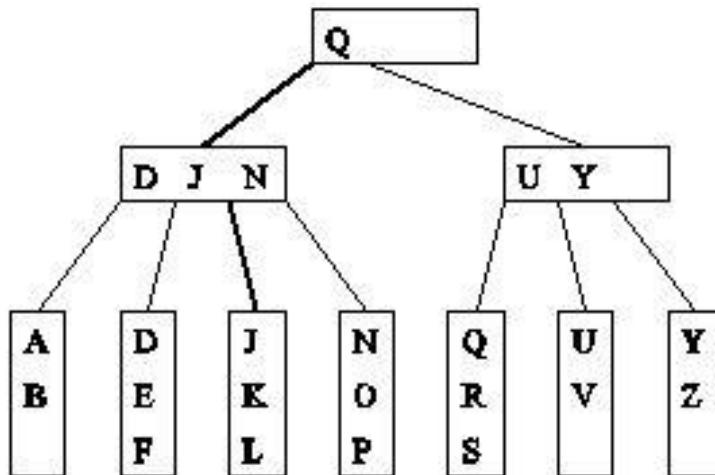
- a.  $O(n^2)$
  - b.  $O(n \log n)$
  - c.  $O(n)$
  - d.  $O(2^n - 1)$
  - e. none of the above.

$$\sum_{i=1}^{n-1} \sum_{j=i+1}^n 1 = \sum_{i=1}^{n-1} i + \sum_{i=1}^{n-1} i + 1 + 1 = \sum_{i=1}^{n-1} 3i + 2 = 3(n-1) + 2 = 3n - 1 = O(n)$$

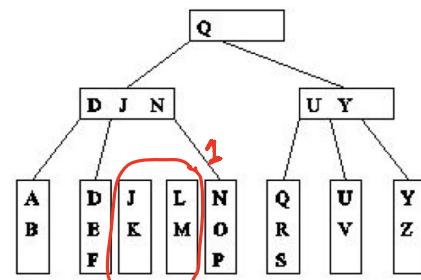
- ### 3. The big-O notation

- a. Can compare algorithms in the same complexity class
  - b. Is an upper bound on the asymptotic complexity of the program
  - c. Is a bottom bound on the asymptotic complexity of the program
  - d. Provide a measure which is valid for different operating systems, compilers and CPUs

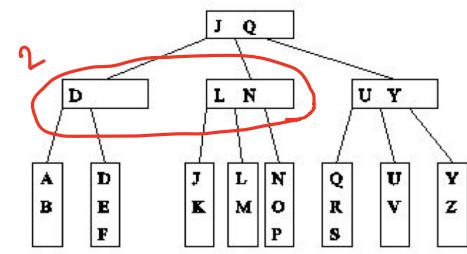
4. Inserting M to the following B+ tree will result in how many splittings?



- a. 0
- b. 1
- c. 2**
- d. 3
- e. 4

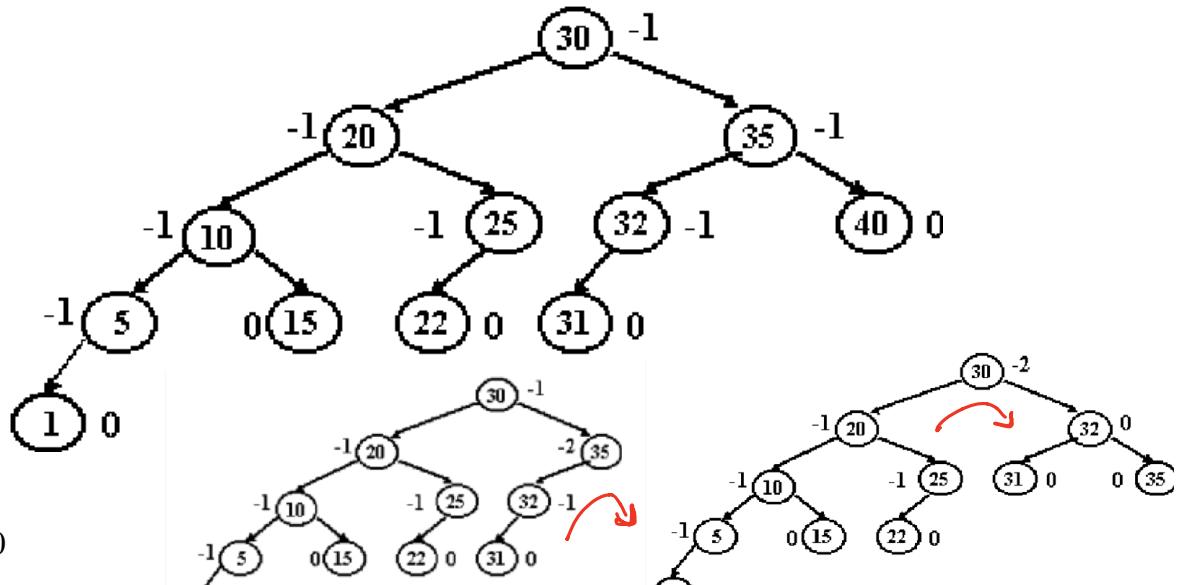


After adding M we see the first split



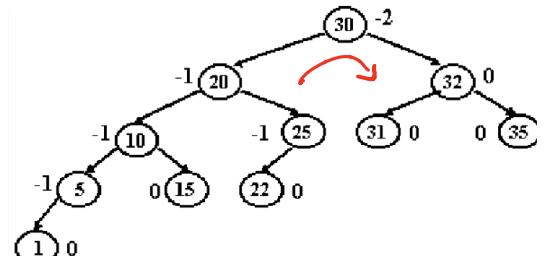
and finally after we perform the operations  
we see the second split

5. Deleting 40 from the following tree will result in how many single rotations?

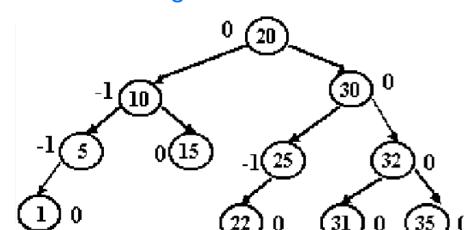


- a. 0
- b. 1
- c. 2**
- d. 3
- e. 4

First, Right rotation this is the first  
single rotation



Second, Right rotation this is the second  
single rotation



Finally, the tree is balanced

**Q2. [35 points] (Graphs):**

A. Consider the following weighted directed graph G:

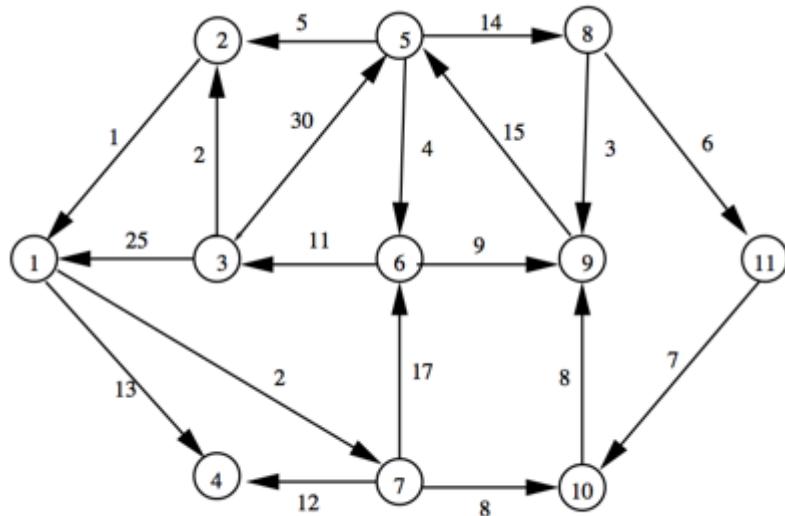
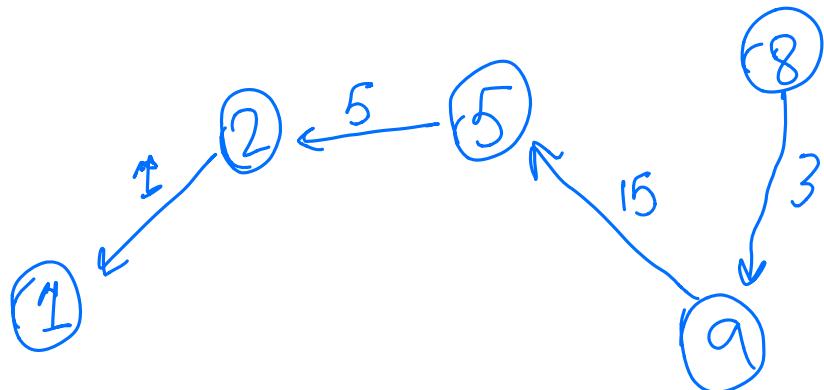


Figure 4

Apply the Dijkstra algorithm on G starting from **vertex 8**:

- B. Show how the table can be used to find the shortest path between vertices 8 and 1.



- C. Can the table be used to find the shortest path starting from vertex 1 going to vertex 11?

No we can't

- D. Fill in the following table with the big-O complexity of each operation

Operation / Data Structure	Adjacency Matrix	Adjacency List
Is there an edge from x to y	$O(1)$	$O(n)$
Edge Insertion	$O(1)$	$O(n)$
Edge deletion	$O(1)$	$O(n)$
Get successor vertices of vertex x	$O(n)$	$O(n)$
Get predecessor vertices of vertex x	$O(n)$	$O(n+m)$
Visit all edges	$O(n^2)$	$O(n+m)$
Space complexity	$O(n^2)$	$O(n+m)$

E. Use Prim's algorithm to find a minimum spanning tree in the same graph.

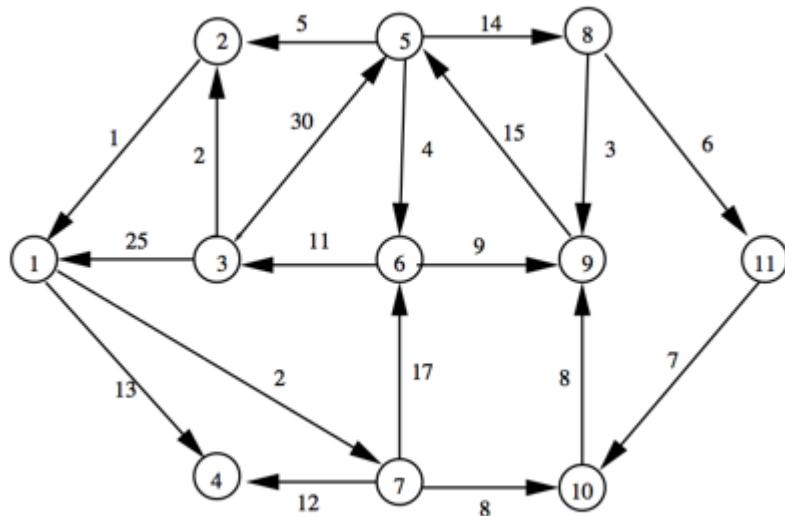
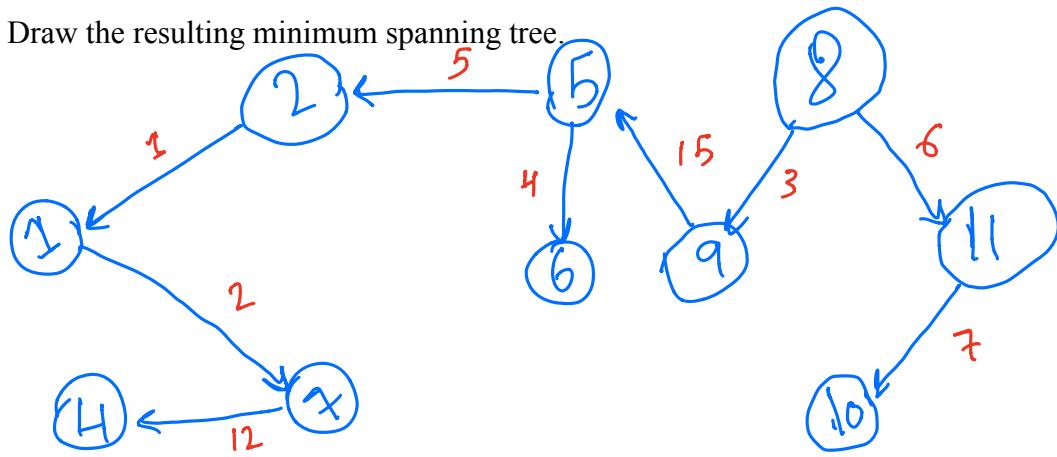


Figure 4

	Initially	1	2	3	4	5	6	7	8	9	10	11	Weight	V1
active		8	9	11	10	5	6	2	1	7	3	4		
1	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	1	1	#	#	#	1	2
2	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	5	5	5	#	#	#	#	5	5
3	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	15	11	11	11	11	11	#	11	6
4	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	15	15	13	12	12	12	12	12	7
5	$\infty$	$\infty$	15	15	15	15	#	#	#	#	#	#	15	9
6	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	4	4	#	#	#	#	#	4	5
7	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	10	8	2	2	#	#	#	2	1
8	0	0	#	#	#	#	#	#	#	#	#	#	0	1
9	$\infty$	3	3	#	#	#	#	#	#	#	#	#	3	8
10	$\infty$	$\infty$	$\infty$	7	7	#	#	#	#	#	#	#	7	11
11	$\infty$	6	6	6	#	#	#	#	#	#	#	#	6	8

F. Draw the resulting minimum spanning tree.



Consider inserting the following keys:

33, 34, 31, 20, 21, 22, 44, 41, 8

respectively, into a hash table of size 11, using open addressing and hash function:

$$h(key) = key \% 11$$

- A. Use quadratic probing as a collision resolution policy with  $c(i) = \pm i^2$   
Show the hash table after the insertions, showing all your work.

0	1	2	3	4	5	6	7	8	9	10
33	34		21	22		8	44	41	31	20

$$h_i(key) = (h(key) \pm i^2) \% 11 \quad i = 0, 1, 2, 3, 4$$

$$h_0(33) = (33 \% 11) \% 11 = 0$$

$$h_0(34) = (34 \% 11) \% 11 = 1$$

$$h_0(31) = (31 \% 11) \% 11 = 9$$

$$h_0(20) = (20 \% 11) \% 11 = 9 \text{ Collision!!}$$

$$h_1(20) = (9 + 1^2) \% 11 = 10$$

$$h_0(21) = (21 \% 11) \% 11 = 10 \text{ Collision!!}$$

$$h_1(21) = (10 + 1^2) \% 11 = 8 \text{ Collision!!}$$

$$h_1(21) = (10 - 1^2) \% 11 = 9 \text{ Collision!!}$$

$$h_2(21) = (10 + 2^2) \% 11 = 3$$

$$h_0(22) = (22 \% 11) \% 11 = 0 \text{ Collision!!}$$

$$h_1(22) = (0 + 1^2) \% 11 = 1 \text{ Collision!!}$$

$$h_2(22) = (0 - 1^2) \% 11 = -1$$

$$\text{Normalize: } (-1 + 11) \% 11 = 10 \text{ Collision!!}$$

$$h_2(22) = (0 + 2^2) \% 11 = 4$$

$$h_0(44) = (44 \% 11) \% 11 = 0 \text{ Collision!!}$$

$$h_1(44) = (0 + 1^2) \% 11 = 1 \text{ Collision!!}$$

$$h_1(44) = (0 - 1^2) \% 11 = -1$$

$$\text{Normalize: } (-1 + 11) \% 11 = 10 \text{ Collision!!}$$

$$h_2(44) = (0 + 2^2) \% 11 = 4 \text{ Collision!!}$$

$$h_{-2}(44) = (0 - 2^2) \% 11 = -4$$

$$\text{Normalize: } (-4 + 11) \% 11 = 7$$

$$h_0(41) = (41 \% 11) \% 11 = 8$$

$$h_0(8) = (8 \% 11) \% 11 = 8 \text{ Collision!!}$$

$$h_1(8) = (8 + 1^2) \% 11 = 9 \text{ Collision!!}$$

$$h_1(8) = (8 - 1^2) \% 11 = 7 \text{ Collision!!}$$

$$h_2(8) = (8 + 2^2) \% 11 = 1 \text{ Collision!!}$$

$$h_2(8) = (8 - 2^2) \% 11 = 4 \text{ Collision!!}$$

$$h_3(8) = (8 + 3^2) \% 11 = 6$$

B. Use double hashing as a collision resolution policy with

$$h_p(key) = 1 + key \% 10$$

Show the hash table after the insertions, showing all your work.

0	1	2	3	4	5	6	7	8	9	10
33	34		21	8	44	22		41	31	20

$$h_i(key) = (h_0(key) + i * h_p(key)) \% 11 \quad i = 0, 1, \dots, 9$$

$$h_0(33) = (33 \% 11) \% 11 = 0$$

$$h_0(34) = (34 \% 11) \% 11 = 1$$

$$h_0(31) = (31 \% 11) \% 11 = 9$$

$$h_0(20) = (20 \% 11) \% 11 = 9 \quad \text{Collision!!}$$

$$h_p(20) = 1 + (20 \% 10) = 1$$

$$h_1(20) = (9 + 1 \% 1) \% 11 = 10$$

$$h_0(21) = (21 \% 11) \% 11 = 10 \quad \text{Collision!!}$$

$$h_p(21) = 1 + (21 \% 10) = 2$$

$$h_1(21) = (10 + 1 \% 2) \% 11 = 1 \quad \text{Collision!!}$$

$$h_2(21) = (10 + 2 \% 2) \% 11 = 3$$

$$h_0(22) = (22 \% 11) \% 11 = 0 \quad \text{Collision!!}$$

$$h_p(22) = 1 + (22 \% 10) = 3$$

$$h_1(22) = (0 + 1 \% 3) \% 11 = 3 \quad \text{Collision!!}$$

$$h_2(22) = (0 + 2 \% 3) \% 11 = 6$$

$$h_0(44) = (44 \% 11) \% 11 = 0 \quad \text{Collision!!}$$

$$h_p(44) = 1 + 44 \% 10 = 5$$

$$h_1(44) = (0 + 1 \% 5) \% 11 = 5$$

$$h_0(41) = (41 \% 11) \% 11 = 8$$

$$h_0(8) = (8 \% 11) \% 11 = 8 \quad \text{Collision!!}$$

$$h_p(8) = 1 + (8 \% 10) = 9$$

$$h_1(8) = (8 + 1 \% 9) \% 11 = 6 \quad \text{Collision!!}$$

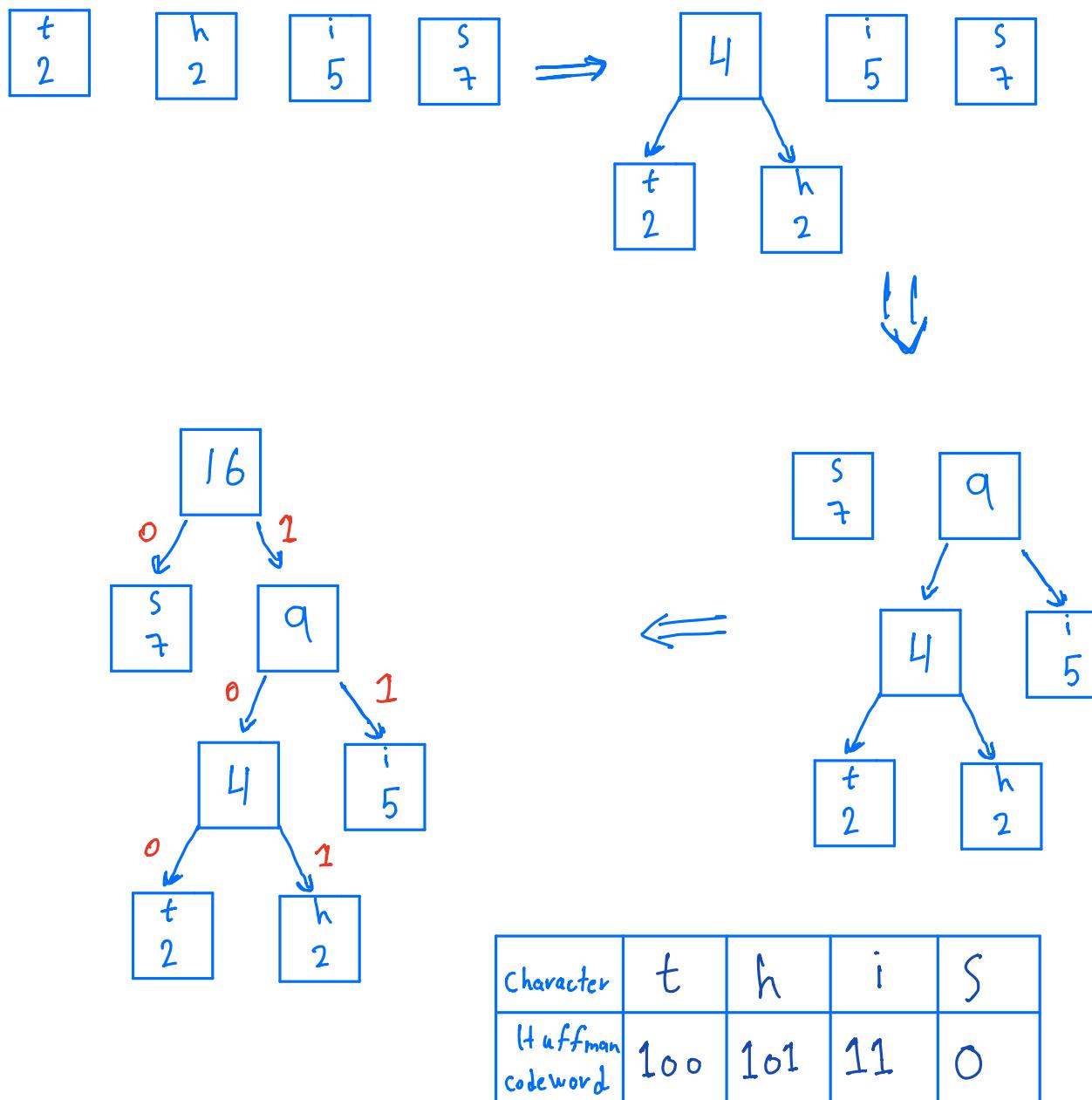
$$h_2(8) = (8 + 2 \% 9) \% 11 = 4$$

**Q.5 [20 points]: (Compression)**

- a) [6 points] Using Huffman coding, show the resulting Huffman coding tree for compressing the following message. Make sure you show all your work.

Char	t	h	i	s
Freq	2	2	5	7

thisisthisisisss



- b) [4 points] Compute the compression ratio, showing your work. Make sure you state any assumptions.

$$\text{Number of bits for the Compressed message} = (3*2) + (3*2) + (2*5) + (1*7) = 29$$

$$\text{Number of bits for the transmitted file} = 29 + (4*8) + 9 + 2 = 72$$

$$\text{Number of bits for the UnCompressed message} = 16 * 8 = 128$$

$$\text{Compression ratio} = \frac{128}{72} = 1.777$$

Should be 3, you need 3 bits to represent number 4

- c) [6 points] Compress the following message using LZ78. Make sure you show all your work:

thisisthisisisss

Output	Index	string
(0,t)	1	t
(0,h)	2	h
(0,i)	3	i
(0,s)	4	s
(3,s)	5	is
(1,h)	6	th
(5,i)	7	isi
(4,i)	8	si
(4,s)	9	ss
(4, )	10	s

Codeword	(0,t)	(0,h)	(0,i)	(0,s)	(3,s)	(1,h)	(5,i)	(4,i)	(4,s)	(4, )
index	1	2	3	4	5	6	7	8	9	10
Bits	$(1+8)$	$(1+8)$	$(2+8)$	$(2+8)$	$(3+8)$	$(3+8)$	$(3+8)$	$(3+8)$	$(4+8)$	$(4+8)$

$$\text{Sum} = 106 \text{ bits}$$

- d) [4 points] Compute the compression ratio, showing your work. Make sure you state any assumptions.

$$\text{Number of bits for the Uncompressed string} = 16 * 8 = 128$$

$$\text{Compression ratio} = \frac{128}{106} = 1.207$$

## Quick Reference Sheet

```

public class SLLNode<T> {
    public T info;
    public SLLNode<T> next;
}
public SLLNode();
public SLLNode(T el)
public SLLNode(T el, SLLNode<T> ptr);
}

public class SLL<T> {
    protected SLLNode<T> head, tail;
    public SLL();
    public boolean isEmpty();
    public void addToHead(T el);
    public void addToTail(T el);
    public T deleteFromHead();
    public T deleteFromTail();
    public void delete(T el);
    public void printAll();
    public boolean isInList(T el);
}

public class DLLNode<T> {
    public T info;
    public DLLNode<T> next, prev;
}
public DLLNode();
public DLLNode(T el);
public DLLNode(T el, DLLNode<T> n,
               DLLNode<T> p);
}

public class DLL<T> {
    private DLLNode<T> head, tail;
    public DLL();
    public boolean isEmpty();
    public void setToNull();
    public void addToHead(T el);
    public void addToTail(T el);
    public T deleteFromHead();
    public T deleteFromTail();
    public void delete(T el);
    public void printAll();
    public boolean isInList(T el);
}

```

```

public class Queue<T> {
    private ...; // array or linked list
}
public Queue();
public void clear();
public boolean isEmpty();
public T firstEl();
public T dequeue();
public void enqueue(T el);
public String toString();
}

public class BSTNode<T extends Comparable<? super T>> {
    protected T el;
    protected BSTNode<T> left, right;
}
public BSTNode();
public BSTNode(T el);
public BSTNode(T el, BSTNode<T> lt,
               BSTNode<T> rt);
}

public class BST<T extends Comparable<? super T>> {
    protected BSTNode<T> root = null;
}
public BST();
protected void visit(BSTNode<T> p);
protected T search(T el);
public void breadthFirst();
public void preorder();
public void inorder();
public void postorder();
protected void inorder(BSTNode<T> p);
protected void preorder(BSTNode<T> p);
protected void postorder(BSTNode<T> p);
public void deleteByCopying(T el);
public void deleteByMerging(T el);
public void iterativePreorder();
public void iterativeInorder();
public void iterativePostorder2();
public void iterativePostorder();
public void MorrisInorder();
public void MorrisPreorder();
public void MorrisPostorder();
public void balance(T data[], int first,
                   int last);
public void balance(T data[]);
public void insert(T el)
}

```

$$\sum_{i=1}^n i = \frac{n(n+1)}{2}, \quad \sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}, \quad \sum_{i=1}^n i^3 = \left( \frac{n(n+1)}{2} \right)^2,$$

$$\sum_{i=0}^n x^i = \frac{x^{n+1}-1}{x-1}, \quad 2^{\lg n} = n, \quad \lg ab = \lg a + \lg b, \quad \lg a^b = b \lg a$$